

Studies on Dielectric Permittivities, Refractive Indices for 1,1'-Bicyclohexyl Liquid Crystals in the Nematic and Isotropic Phases

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The dielectric permittivities $\epsilon_{\parallel}$ and $\epsilon_{\perp}$ and the refractive indices n_e , n_o of five 4-cyano-4'-alkyl-1,1'-bicyclohexyls (CCH 2, CCH 3, CCH 4, CCH 5, CCH 7 where 2, 3, 4, 5, 7 means ethyl, propyl, butyl, pentyl, heptyl respectively) have been measured at different temperatures in the nematic and isotropic phases. The orientational order parameter from the refractive indices data, calculated from (1) Vuks' method and (2) Neugebauer's method were in good agreement. At any reduced temperature, the order parameter for CCH 2 is largest and that of CCH 7 is smallest and those for the others are in between them. Unlike for cyanobiphenyls or cyclohexylbenzenes, the dielectric permittivity $\epsilon_{\parallel}$ is obtained for $\vec{E} \perp \vec{H}$ and $\epsilon_{\perp}$ for $\vec{E} \parallel \vec{H}$, where $\vec{E}$ is the electric and $\vec{H}$ is the magnetic field, and has been explained as due to these molecules having negative diamagnetic anisotropy. The dielectric anisotropy, $\Delta\epsilon$ and optical anisotropy Δn for all the CCH's is much less than that of the corresponding CB or PCH molecules. All the CCH's show pretransitional permittivity just above the transition temperature T_{NI} .

Dielectric permittivities and refractive indices of liquid crystals are required for their selection for practical uses. The data for dielectric permittivities and refractive indices for alkylcyanobiphenyls,¹⁻³⁾ cyclohexylbenzenes,⁴⁾ phenylcyclohexanecarboxylates⁵⁾ have been reported earlier. Such data for CCH's are rather scanty. The object of the present investigations were to study how the dielectric properties and refractive indices change when both the phenyl rings are replaced by cyclohexyl rings.

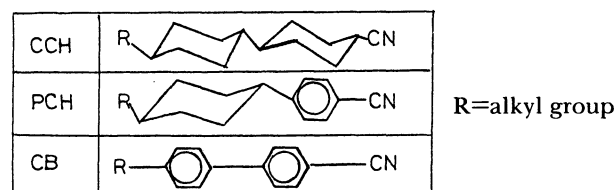
Studies on the temperature dependence of dielectric permittivities in the isotropic phase for nematics with strong dipole moments show pretransitional effects while in nonpolar nematics pretransitional effect is absent.^{5,6)} It was thought worthwhile to study the pretransitional effects in dielectric permittivity in the isotropic phase of 1,1'-bicyclohexyl liquid crystals. The results are discussed in this paper.

Experimental

Five CCH liquid crystals (CCH 2, CCH 3, CCH 4, CCH 5,

CCH 7) procured from E. Merck, Germany were used in the investigations without further purification. Mesomorphic range of the samples,

Sample	Nematic range/°C
CCH 2 (4-cyano-4'-ethyl-1,1'-bicyclohexyl)	46—49
CCH 3 (4-cyano-4'-propyl-1,1'-bicyclohexyl)	50—80
CCH 4 (4-cyano-4'-butyl-1,1'-bicyclohexyl)	54—79
CCH 5 (4-cyano-4'-pentyl-1,1'-bicyclohexyl)	62—85
CCH 7 (4-cyano-4'-heptyl-1,1'-bicyclohexyl)	71—83



Measurement of Refractive Indices. The method of measurement of the refractive indices n_e , n_o for the extraordinary and ordinary rays with the help of ABBE refractometer and density measurements by means of capillary tube were de-

Table 1. Refractive Indices, Density, Polarizabilities and Order Parameter for CCH

$T/^{\circ}\text{C}$	$\rho/\text{g ml}^{-1}$	n_o	n_e	$\bar{\alpha}$	Vuks' method			Neugebauer's method		
				$\text{\AA}^3$	$\alpha_o/\text{\AA}^3$	$\alpha_e/\text{\AA}^3$	S	$\alpha_o/\text{\AA}^3$	$\alpha_e/\text{\AA}^3$	S
(a) CCH 2										
46	0.925	1.4661	1.4959	26.486	25.822	27.806	0.62	25.903	27.652	0.65
46.5	0.924	1.4661	1.4953	26.498	25.846	27.791	0.60	25.922	27.648	0.64
47	0.923	1.4662	1.4942	26.503	25.878	27.744	0.58	25.950	27.607	0.62
47.5	0.923	1.4663	1.4934	26.507	25.903	27.709	0.56	25.968	27.586	0.60
48	0.922	1.4668	1.4919	26.518	25.959	27.605	0.52	26.025	27.503	0.55
49	0.919	1.4748								
49.5	0.918	1.4746								
50	0.918	1.4742								
50.5	0.917	1.4741								
51	0.917	1.4740								
53.5	0.915	1.4729			$\alpha_{\perp}=$	$\alpha_{\parallel}=$		$\alpha_{\perp}=$	$\alpha_{\parallel}=$	
55.5	0.913	1.4720			25.532	28.726		25.703	28.384	

Table 1. (Continued)

$T/^{\circ}\text{C}$	$\rho/\text{g ml}^{-1}$	n_o	n_c	$\bar{\alpha}$	Vuks' method			Neugebauer's method		
				$\text{\AA}^3$	$\alpha_o/\text{\AA}^3$	$\alpha_c/\text{\AA}^3$	S	$\alpha_o/\text{\AA}^3$	$\alpha_c/\text{\AA}^3$	S
(b) CCH 3										
58.5	0.915	1.4590	1.5056	28.416	27.303	30.644	0.65	27.479	30.291	0.66
62	0.912	1.4578	1.5029	28.407	27.326	30.569	0.63	27.492	30.238	0.64
64	0.910	1.4575	1.5014	28.431	27.375	30.537	0.61	27.528	30.239	0.63
66.5	0.908	1.4567	1.4991	28.422	27.401	30.461	0.59	27.556	30.154	0.61
68.5	0.906	1.4564	1.4968	28.428	27.453	30.375	0.56	27.597	30.090	0.58
70.5	0.905	1.4560	1.4949	28.442	27.499	30.317	0.54	27.622	30.081	0.57
73	0.902	1.4553	1.4930	28.452	27.538	30.275	0.53	27.669	30.020	0.55
76	0.900	1.4546	1.4900	28.452	27.594	30.171	0.50	27.731	29.895	0.51
78	0.898	1.4545	1.4878	28.469	27.658	30.084	0.47	27.776	29.854	0.49
80.5	0.896	1.4548	1.4834	28.464	27.764	29.855	0.40	27.865	29.662	0.42
82.5	0.889	1.4635								
85	0.887	1.4625								
87	0.885	1.4615			$\alpha_{\perp}=$	$\alpha_{\parallel}=$		$\alpha_{\perp}=$	$\alpha_{\parallel}=$	
89	0.884	1.4605			26.910	32.093		27.212	31.490	
(c) CCH 4										
56	0.9109	1.4650	1.5081	30.503	29.407	32.695	0.64	29.601	32.305	0.61
58	0.9092	1.4642	1.5070	30.517	29.418	32.692	0.64	29.572	32.409	0.64
60	0.9066	1.4635	1.5048	30.540	29.481	32.645	0.62	29.607	32.404	0.63
64	0.9041	1.4616	1.5026	30.516	29.466	32.606	0.61	29.576	32.394	0.63
68	0.9005	1.4600	1.4998	30.518	29.496	32.583	0.60	29.678	32.199	0.63
76	0.8928	1.4554	1.4973	30.573	29.477	32.744	0.61	29.605	32.507	0.57
78	0.8909	1.4558	1.4939	30.582	29.593	32.560	0.58	29.742	32.267	0.57
79	0.8858	1.4680								
80	0.8850	1.4676								
82	0.8836	1.4663								
83	0.8826	1.4650								
85	0.8812	1.4644								
87	0.8799	1.4640								
90	0.8783	1.4620			$\alpha_{\perp}=$	$\alpha_{\parallel}=$		$\alpha_{\perp}=$	$\alpha_{\parallel}=$	
92	0.8762	1.4616			29.013	34.152		29.255	33.666	
(d) CCH 5										
68	0.906	1.4580	1.5093	32.516	30.796	34.960	0.64	31.018	35.514	0.64
72	0.902	1.4568	1.5061	32.198	30.861	34.876	0.62	31.076	34.440	0.61
76	0.898	1.4560	1.5020	32.218	30.963	34.726	0.58	31.151	34.353	0.58
78	0.897	1.4560	1.4991	32.226	31.048	34.580	0.54	31.223	34.231	0.55
81	0.894	1.4568	1.4931	32.238	31.231	34.259	0.46	31.396	33.923	0.46
83	0.892	1.4575	1.4823	32.252	31.378	33.999	0.40	31.511	33.733	0.41
85	0.884	1.4675								
86	0.883	1.4665								
87	0.883	1.4660								
88	0.882	1.4655								
89	0.881	1.4650			$\alpha_{\perp}=$	$\alpha_{\parallel}=$		$\alpha_{\perp}=$	$\alpha_{\parallel}=$	
92	0.880	1.4640			30.327	36.850		30.672	36.161	
(e) CCH 7										
71	0.893	1.4558	1.5009	35.858	34.487	38.600	0.52	34.713	38.157	0.54
72	0.892	1.4554	1.4997	35.843	34.500	38.539	0.51	34.716	38.103	0.53
73	0.891	1.4552	1.4980	35.843	34.542	38.449	0.49	34.751	38.026	0.52
74	0.890	1.4550	1.4966	35.842	34.573	38.374	0.48	34.758	38.009	0.51
75	0.889	1.4548	1.4952	35.840	34.607	38.302	0.47	34.786	37.948	0.50
76	0.888	1.4546	1.4936	35.838	34.652	38.220	0.45	34.849	37.816	0.47
77	0.887	1.4544	1.4919	35.822	34.678	38.114	0.43	34.859	37.748	0.45
78	0.886	1.4542	1.4905	35.826	34.717	38.102	0.43	34.894	37.689	0.44
79	0.885	1.4540	1.4891	35.840	34.764	37.987	0.40	34.915	37.689	0.44
80	0.884	1.4538	1.4874	35.841	34.810	37.902	0.39	34.959	37.605	0.42
81	0.883	1.4537	1.4859	35.851	34.862	37.828	0.37	35.004	37.547	0.40
82	0.880	1.4536								
84	0.877	1.4625								
87	0.875	1.4604			$\alpha_{\perp}=$	$\alpha_{\parallel}=$		$\alpha_{\perp}=$	$\alpha_{\parallel}=$	
89	0.873	1.4592			33.311	41.229		33.833	40.184	

Table 2. Dielectric Permittivities of CCH

$T/^{\circ}\text{C}$	$\epsilon_{\parallel}$	ϵ_{iso}	$\epsilon_{\perp}$	$\bar{\epsilon}$	$T/^{\circ}\text{C}$	$\epsilon_{\parallel}$	ϵ_{iso}	$\epsilon_{\perp}$	$\bar{\epsilon}$
(a) CCH 2					82		7.072		
46.5	9.85		5.696	7.081	83		7.108		
47	9.782		5.757	7.099	85		7.159		
47.5	9.760		5.869	7.166	87		7.152		
48	9.684		5.892	7.156	90		7.146		
48.5	9.440		5.939	7.106	92		7.110		
50		7.503			(d) CCH 5				
51		7.562			51	8.586		4.365	5.772
52		7.603			56	8.910		4.371	5.884
53		7.624			60	8.992		4.479	5.983
54		7.607			65	9.146		4.631	6.136
55		7.532			69	9.214		4.723	6.220
56		7.503			73	9.251		4.753	6.252
60		7.382			77	9.279		4.832	6.314
(b) CCH 3					81	9.333		4.951	6.412
58	9.419		4.673	6.255	84	8.752		5.412	6.525
60	9.598		4.732	6.354	85		6.596		
62	9.725		4.863	6.484	87		6.779		
64	10.015		4.905	6.608	88		7.173		
66.5	10.184		5.099	6.794	89		7.341		
68.5	10.112		5.185	6.827	90		7.337		
70.5	10.094		5.385	6.955	91		7.328		
73	9.998		5.459	6.972	93		7.319		
76	9.968		5.593	7.051	96		7.298		
78	9.953		5.702	7.119	(e) CCH 7				
79	9.490		5.722	6.978	74	7.169		3.888	4.982
80.5		7.855			75	7.181		3.963	5.036
82.5		7.916			76	7.175		4.020	5.072
83		8.207			77	7.182		4.045	5.091
84		8.024			78	7.155		4.067	5.096
85		7.959			79	7.132		4.050	5.077
86		7.554			80	6.939		4.037	5.004
88		7.463			82	6.919		4.022	4.988
90		7.340			83	6.490		4.036	4.854
(c) CCH 4					84	6.444		3.985	4.805
56	8.871		4.361	5.864	86	5.895		4.246	4.796
58	8.876		4.404	5.895	87		4.891		
60	9.119		4.386	5.964	88		4.919		
64	9.119		4.592	6.101	89		4.925		
68	9.120		4.635	6.130	90		4.873		
72	9.117		4.893	6.301	91		4.849		
76	9.037		5.049	6.378	93		4.821		
78	8.934		5.467	6.623	94		4.806		
79	8.869		5.472	6.604	96		4.799		
80	8.741		5.474	6.563	98		4.796		

scribed elaborately in an earlier publication.⁷⁾

Measurement of Dielectric Permittivities. The dielectric permittivities $\epsilon_{\parallel}$ and $\epsilon_{\perp}$ polarized parallel and perpendicular to the long molecular axes of the liquid crystals were measured at 1 kHz with a GR-1620 capacitance bridge using a capacitor of stainless steel electrodes of radius 1 cm separated by a 1 mm thick Teflon spacer. A magnetic field of 1.0 T was used to align the molecules of the liquid crystals parallel and perpendicular to the electrode surfaces. The temperature of the sample was measured with a thermocouple mounted directly on one of the electrodes. The temperature of the cell was maintained constant within $\pm 0.02^{\circ}\text{C}$ by means of a thermostat. The cell was calibrated with freshly distilled toluene and chlorobenzene and the values agree to 0.1% of the standard value.

Results

The experimental values of refractive indices n_e , n_o and the densities of the liquid crystals at different temperatures are given in Table 1. The effective polarizabilities α_e and α_o in the nematic phase calculated by using two methods Vuks⁸⁾ and Neugebauer⁹⁾ are included in Table 1. The principal polarizabilities $\alpha_{\parallel}$ and $\alpha_{\perp}$ parallel and perpendicular to the long axis of the molecules in the crystalline state were obtained from Hallers' et al.¹⁰⁾ graphical method. The orientational order parameters S were calculated from the relation $S = (\alpha_e - \alpha_o) / (\alpha_{\parallel} - \alpha_{\perp})$ and are included in Table 1.

Table 3a. Values of the Dielectric Anisotropy of CCH Compounds at Different Reduced Temperature

CCH 2		CCH 4		CCH 7	
T/T_{NI}	$\Delta\epsilon$	T/T_{NI}	$\Delta\epsilon$	T/T_{NI}	$\Delta\epsilon$
0.989	4.154	0.927	4.510	0.964	3.281
0.991	4.025	0.932	4.472	0.967	3.218
0.992	3.891	0.949	4.527	0.972	3.137
0.994	3.792	0.961	4.485	0.975	3.088
0.995	3.501	0.972	4.224	0.981	2.902
		0.989	3.467	0.989	2.454
		0.992	3.397	0.997	1.649
		0.994	3.267		

Table 3b. Values of the Dielectric Anisotropy of CB 7, PCH 7, and CCH 7 at Different Reduced Temperature

CB 7		PCH 7		CCH 7	
T/T_{NI}	$\Delta\epsilon$	T/T_{NI}	$\Delta\epsilon$	T/T_{NI}	$\Delta\epsilon$
0.930	12.1	0.930	8.12	0.964	3.28
0.955	11.7	0.954	7.84	0.972	3.14
0.970	11.1	0.967	7.41	0.975	3.09
0.980	10.3	0.980	6.92	0.980	2.90
0.995	8.6	0.990	6.03	0.992	2.46

Table 4a. Values of the Order Parameter of CCH Compounds at Different Reduced Temperature

CCH 2		CCH 4		CCH 7	
T/T_{NI}	S	T/T_{NI}	S	T/T_{NI}	S
0.991	0.65	0.935	0.61	0.969	0.54
0.992	0.64	0.940	0.64	0.971	0.53
0.994	0.62	0.957	0.63	0.977	0.51
0.995	0.60	0.969	0.63	0.980	0.50
0.997	0.55	0.991	0.57	0.983	0.47
				0.989	0.45
				0.994	0.42

Table 4b. Values of the Order Parameter of CB 7, PCH 7, and CCH 7 at Different Reduced Temperature

CB 7		PCH 7		CCH 7	
T/T_{NI}	S	T/T_{NI}	S	T/T_{NI}	S
0.950	0.62	0.948	0.50	0.969	0.54
0.959	0.58	0.954	0.49	0.971	0.53
0.968	0.56	0.967	0.46	0.977	0.51
0.978	0.52	0.979	0.41	0.980	0.50
		0.985	0.39	0.983	0.47
				0.989	0.44
				0.994	0.42

Discussion

The values of the dielectric anisotropy, $\Delta\epsilon$, Table 3b, Fig. 4b for CB,¹¹⁾ PCH,⁴⁾ and CCH compounds in the present paper shows that $\Delta\epsilon$ gradually decreases from CB to PCH to CCH by the progressive replacement of one phenyl ring in PCH and both the phenyl rings in the CCH compounds by cyclohexyl groups. This may be attributed to the decrease in the degree of conjugation.

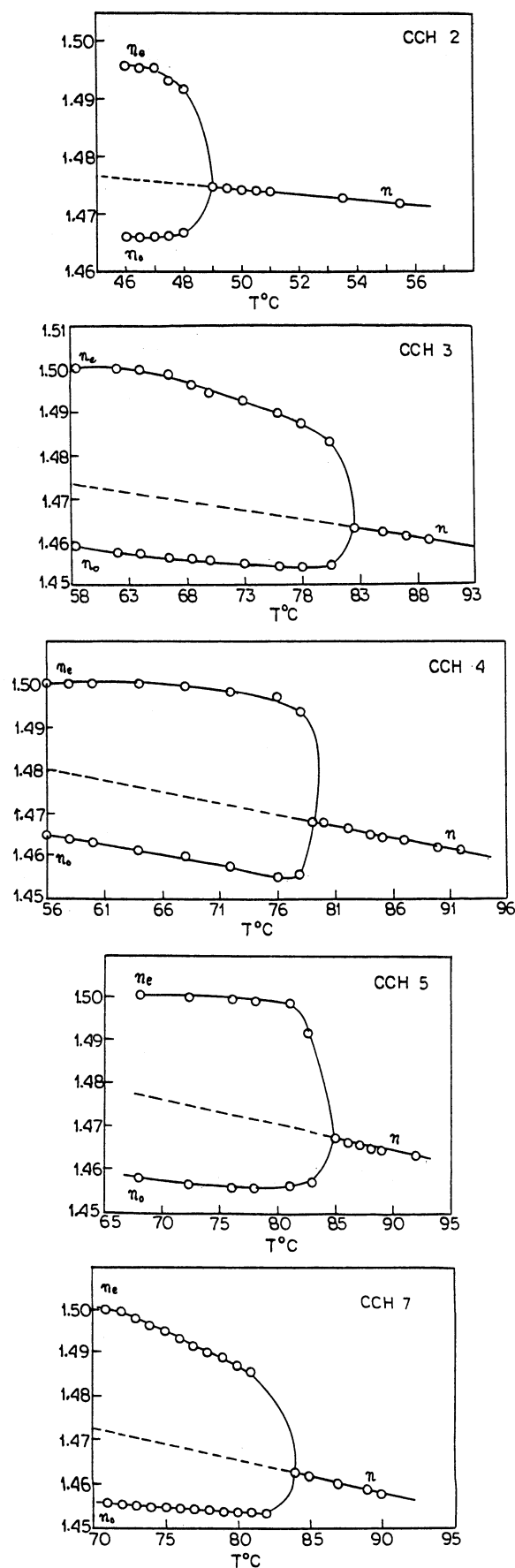


Fig. 1. Refractive index anisotropy plots for CCH 2, CCH 3, CCH 4, CCH 5, CCH 7 respectively.

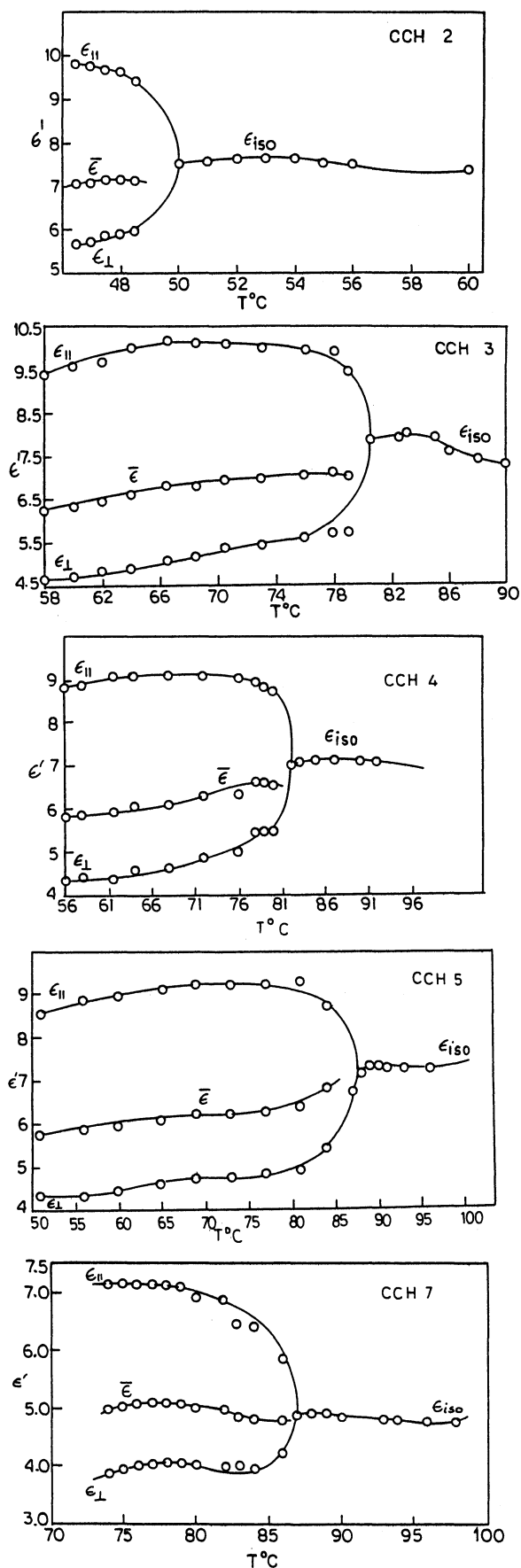


Fig. 2. Dielectric anisotropy plots for CCH 2, CCH 3, CCH 4, CCH 5, CCH 7 respectively.

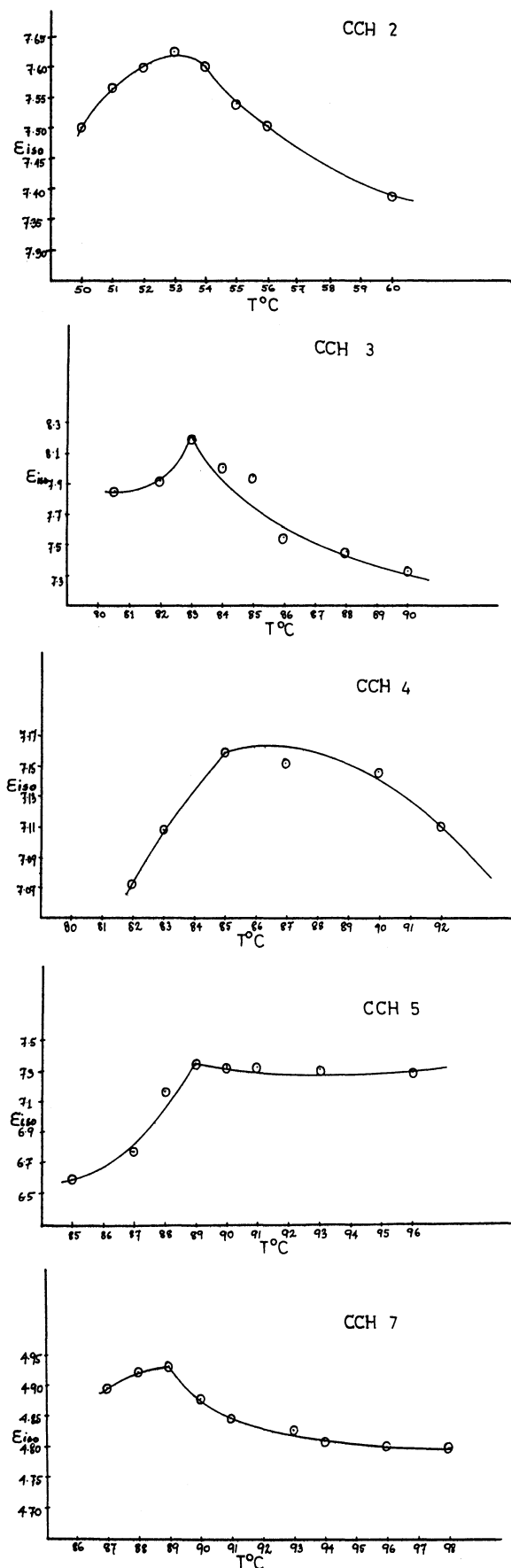


Fig. 3. Pretransition effect plots for CCH 2, CCH 3, CCH 4, CCH 5, CCH 7 respectively.

tion by progressive replacement of phenyl rings. This decrease of conjugation is more pronounced in the CCH compounds which are completely lacking in free π electrons.

The values of $\Delta\epsilon$ within the CCH compounds, Table 3a, Fig. 4a, decreases with the increase of chain length which is also found in the case of PCH compounds by Schadt et al.¹¹⁾

Schadt¹¹⁾ found that the experimental data for the PCH compounds hold the relation $\Delta\epsilon(t_r) \propto S(t_r)$, considering only the contribution of the predominant dipolar part of the dielectric polarization to $\Delta\epsilon$, though one would expect that $S(t_r)/T$ should depend on $\Delta\epsilon$. A possible explanation of the result was given¹¹⁾ by a model of antiparallel dipole correlation.

In the case of the CCH compounds (Fig. 5a) the decrease of order parameter at any reduced tempera-

ture, with the increase of alkyl chain length may also be explained from the above relation.

From Table 1a–e, it can be seen that the order parameter S for each of the CCH liquid crystals evaluated from refractive indices and density data using Vuks' and Neugebauer's methods are in good agreement. Figure 5a, a comparison of the order parameter of the CCH liquid crystals at any common reduced temperature, $t_r = T/T_{NI}$, shows that the order parameter of CCH 2 is the largest and that for CCH 7 is the smallest and those for others are in between them. It appears that the larger the alkyl chain length the smaller is the order parameter.

The values of the order parameters at any reduced temperature t_r in CB, is the largest and in PCH is the smallest, Fig. 5b. But in the case of CCH compounds it is nearer to that of the CB compounds but greater than that for PCH. This cannot be explained from the above relation.¹¹⁾

The antiparallel local ordering in CCH compounds found by X-ray measurement¹²⁾ corresponds to the overlap of cyano group, which is quite different from

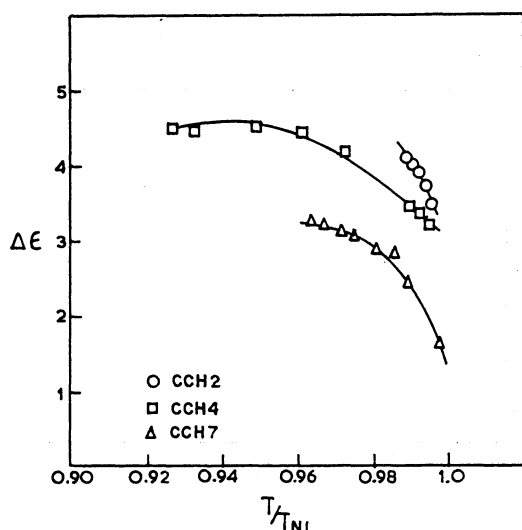


Fig. 4(a). Plots of $\Delta\epsilon$ vs. T/T_{NI} for CCH 2, CCH 4, CCH 7.

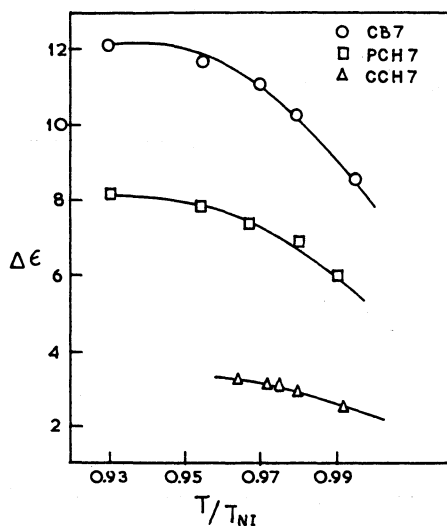


Fig. 4(b). Plots of $\Delta\epsilon$ vs. T/T_{NI} for CB 7, PCH 7, CCH 7.

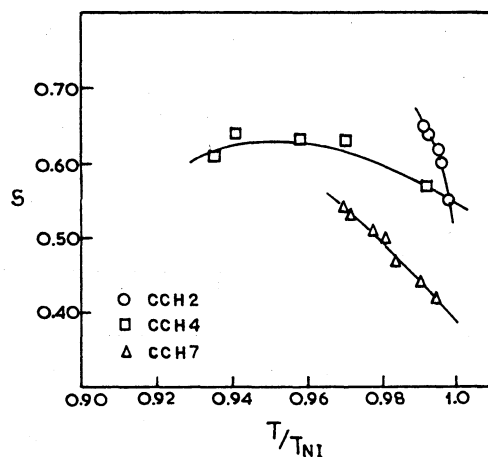


Fig. 5(a). Plots of S vs. T/T_{NI} for CCH 2, CCH 4, CCH 7.

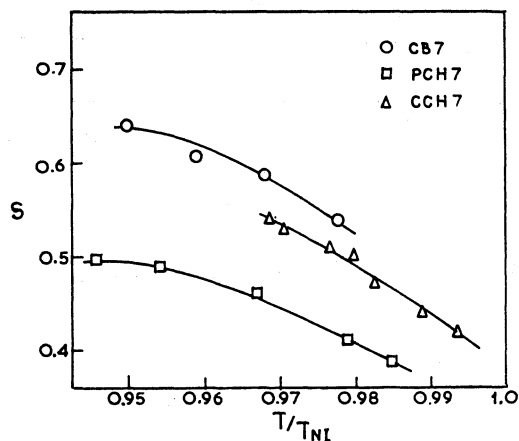


Fig. 5(b). Plots of S vs. T/T_{NI} for CB 7, PCH 7, CCH 7.

the core overlap in the case of CB and PCH compounds. This type of different local ordering in CCH compounds must affect the value of the order parameter and this may be the cause of the unexpected value of the order parameter in the CCH compound.

This type of unexpected observation of the ratio of Bend/splay (k_{33}/k_{11}) value of the elastic constant of the CCH compounds was found by Bradshaw et al.⁵⁾

It is to be noted that for all the CCH liquid crystals, the dielectric permittivity $\epsilon_{\parallel}$ is obtained for $\vec{E} \perp \vec{H}$ and $\epsilon_{\perp}$ is obtained when $\vec{E} \parallel \vec{H}$ unlike the cyanobiphenyls, cyclohexylbenzenes, and other thermotropic liquid crystals, all of which have positive diamagnetic anisotropy. 1,1'-Bicyclohexyls have got negative diamagnetic anisotropy as was shown by Schad¹¹⁾ in CCH 7 ($\Delta\chi = -2 \times 10^{-8} \text{ cm}^3 \text{ g}^{-1}$). The negative diamagnetic anisotropy in CCH 5 was also confirmed by Pohl et al.¹²⁾ from the studies of the dependence of electric threshold voltage and switching time of a twisted layer of CCH 5, with the strength of the magnetic field.

Because of the negative anisotropy of the susceptibility, the CCH molecules orient themselves with the long molecular axis perpendicular to the magnetic field and this is why dielectric permittivity $\epsilon_{\parallel}$ is obtained when $\vec{E} \perp \vec{H}$.

The anisotropy of the dielectric permittivity of the CCH's are shown in Fig. 2a—e. The average value of the dielectric permittivities $\bar{\epsilon}$; shown in Table 2a—e in each case is found to increase with increase in temperature and is discontinuous with the isotropic value ϵ_{iso} at T_{NI} , Fig. 2a—e. This indicates the presence of strong antiparallel local ordering of the CCH molecules in the nematic phase in strongly polar molecules as reported earlier.¹³⁾

Temperature dependence of dielectric permittivity ϵ_{iso} for the CCH liquid crystals in the isotropic phase is shown in Fig. 3a—e. It can be clearly seen that there is

a peak in ϵ_{iso} , a little above the transition temperature T_{NI} . Such pretransition effects in dielectric permittivity in nematics with cyano end groups were reported by Bradshaw and Raynes,⁵⁾ Theon and Menu,⁶⁾ and recently by Krishnakoli et al.¹⁴⁾ The reduced contribution to dielectric permittivity ϵ_{iso} from dipole moment μ was attributed to apparent reduction in μ -values due to formation of dimers in antiparallel local ordering.¹⁵⁾ The pretransition in ϵ_{iso} near T_{NI} showing a maximum was explained as due to appreciable concentration of dimers in a dynamic dimer-monomer equilibrium.

References

- 1) S. Sen, P. Brahma, S. K. Roy, D. K. Mukherjee, and S. B. Roy, *Mol. Cryst. Liq. Cryst.*, **100**, 327 (1983).
- 2) S. Sen, P. Brahma, S. K. Roy, and S. B. Roy, *Acta Physica Polonica*, **A65**, 47 (1984).
- 3) B. R. Ratna and R. Sashidhar, *Pramana*, **6**, 278 (1976).
- 4) S. Sen, K. Kali, S. K. Roy, and S. B. Roy, *Mol. Cryst. Liq. Cryst.*, **126**, 269 (1985).
- 5) M. J. Bradshaw and E. P. Raynes, *Mol. Cryst. Liq. Cryst.*, **L72**, 73 (1981).
- 6) J. Theon and G. Menu, *Mol. Cryst. Liq. Cryst.*, **97**, 163 (1983).
- 7) K. Kali, S. Sen, and S. K. Roy, *Bull. Chem. Soc. Jpn.*, **58**, 3576 (1985).
- 8) M. F. Vuks, *Opt. Spectrosc.*, **20**, 361 (1966).
- 9) H. E. J. Neugebauer, *Can. J. Phys.*, **32**, 1 (1954).
- 10) I. Haller, H. A. Huggins, H. R. Lilienthal, and T. R. McGuire, *J. Phys. Chem.*, **77**, 950 (1973).
- 11) Hp. Schad, G. Baur, and G. Meier, *J. Chem. Phys.*, **71**, 3174 (1979).
- 12) L. Pohl, R. Eidenchink, J. Krause, and G. Weber, *Phys. Lett.*, **65A**, 169 (1978).
- 13) N. V. Madhusudan and S. Chandrasekhar, *Proc. International Conf. Liq. Cryst. Bangalore* (1973), p. 427.
- 14) K. Kali, S. Sen, and S. K. Roy, *Acta Physica Polonica*, in press (1987).
- 15) L. Longa and W. H. de Jeu, *Phys. Rev. A*, **26**, 1632 (1982).